

Technical Drawing with Draftsman



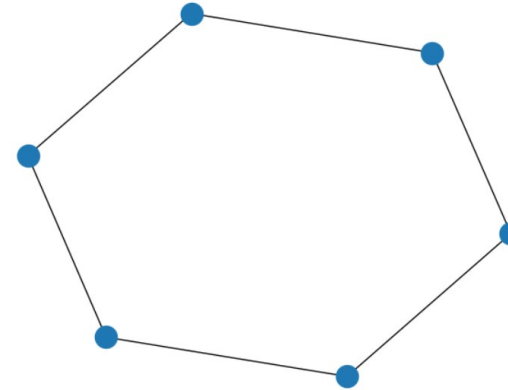
Warm Up: Finde den Unterschied

Frage:

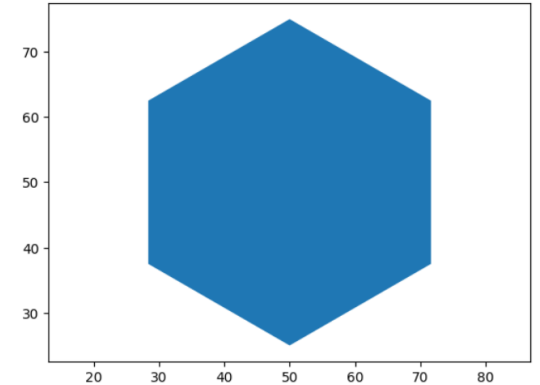
Auf der rechten Seite sind zwei 6-Ecke („Hexagon“) dargestellt:
einmal als Graph, einmal als Polygon.

Welche der folgenden Aussagen sind falsch?

- a) Graph und Polygon bezeichnen dasselbe, d.h. sind identisch.
- b) Ein Graph beschreibt die Topologie, ein Polygon beschreibt die Geometrie.
- c) Ein Polygon ist auch ein Graph.
- d) Ein Graph kann auch Informationen über die Geometrie haben.



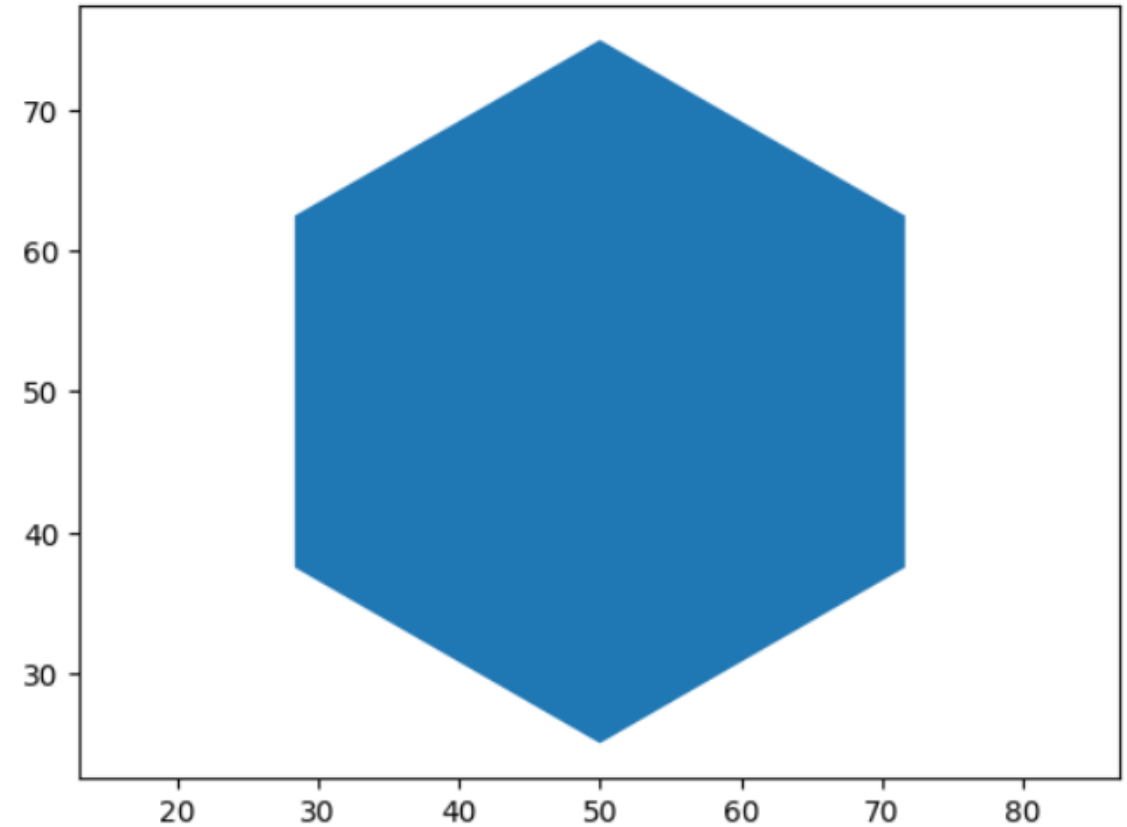
Graph



Polygon

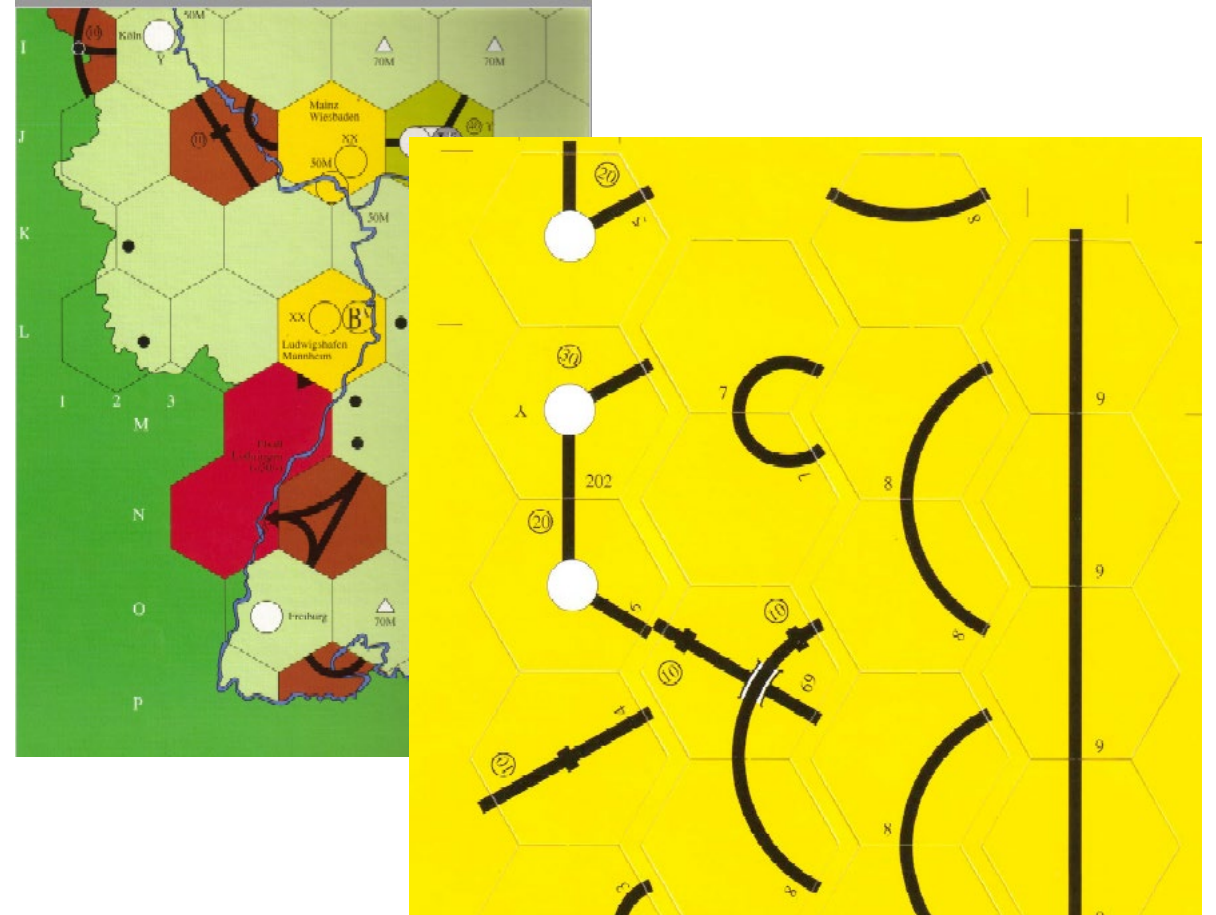
(Technical) Drawing with matplotlib: Patches

- Matplotlib is a very strong toolset.
- It actually allows some kind of „drawing (geometric) shapes“.
- Instead of the expression `shape` matplotlib is using the expression `patch`. Patches are
 - Rectangle
 - Circles
 - Polygon
- Remark: there are better libraries on the market than matplotlib for drawing shapes. Matplotlib is best choice when using Jupyter Notebooks on DataHub.
- Alternative: Qt
 - <https://www.qt.io/> (general information)
 - <https://doc.qt.io/qtforpython-6/index.html> (Python library)



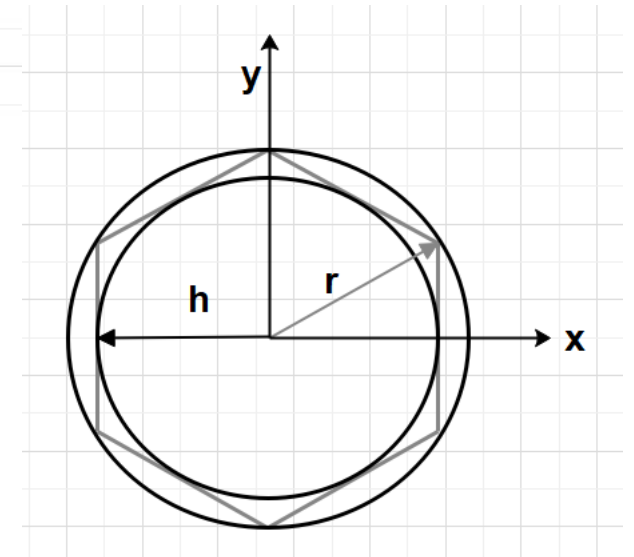
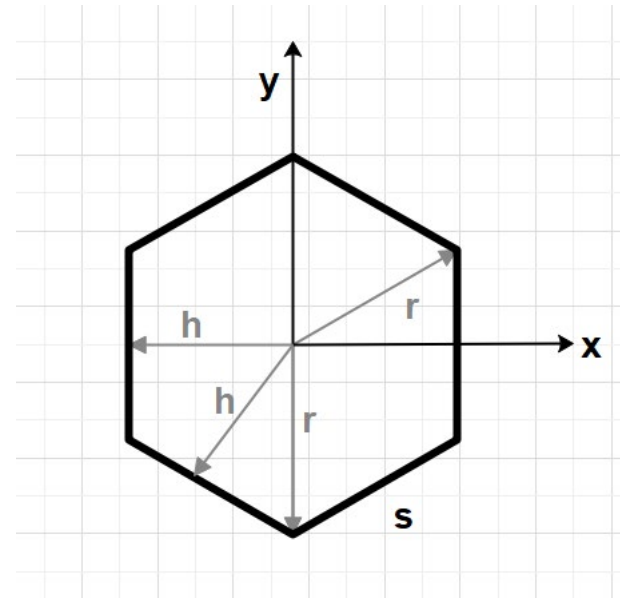
The 18xx Games

- Series of strategy games topic „railroad management“
- Created in the 1990s
- Many versions
 - 1830 US
 - 1835 Germany
 - Many more
- Based on history
- Lot of calculations
- Board is based on hexagon elements with tracks and stations on it.
- Average time for a single game: 10h



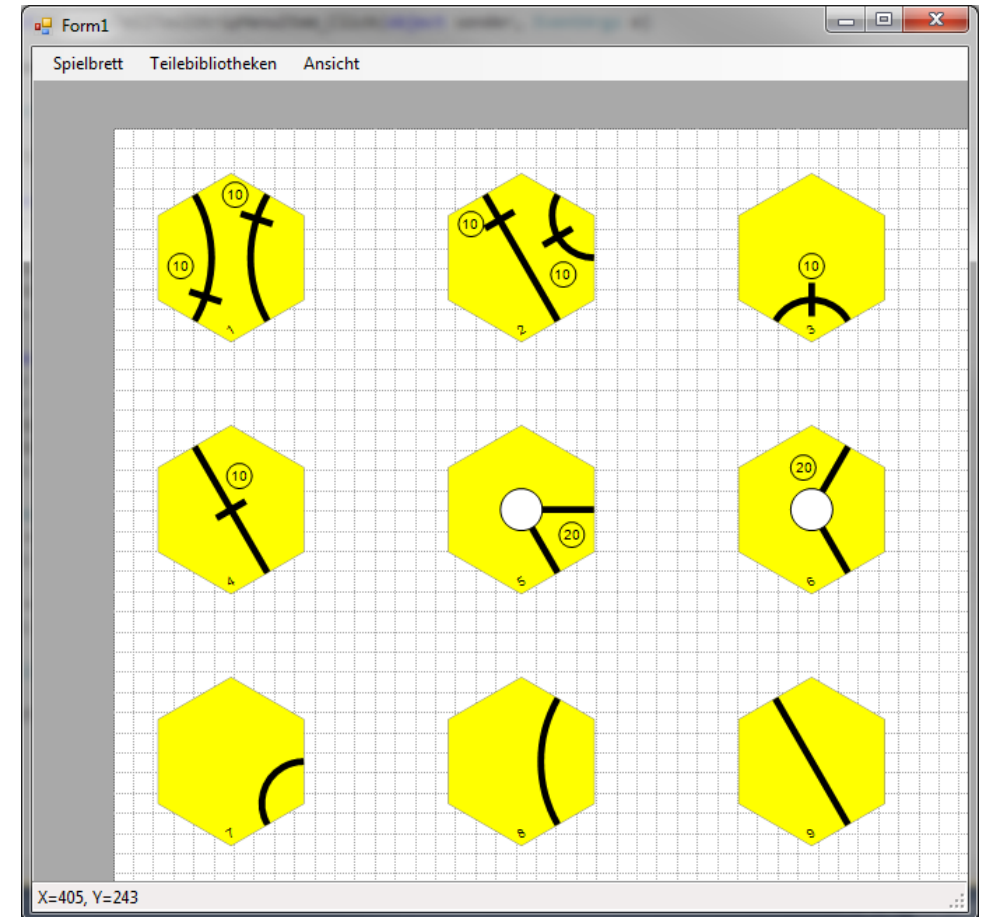
Geometry of a hex-Tile

- The size of the tile is defined by the length of the side: s
- From basic geometry (circle, triangular) we are able to calculate r and h out of s :
 - $r = s$
 - $h = r / 2 * \sqrt{3}$
- The values for r and h are the radii of the inner and outer circle of the hexagon.
- In case we „know“ the coordinates of the center of the hexagon, we are able to calculate the coordinates of the „describing“ elements
 - the corners
 - the middles of the edges
- We need these values for drawing the shape as well drawing the tracks.



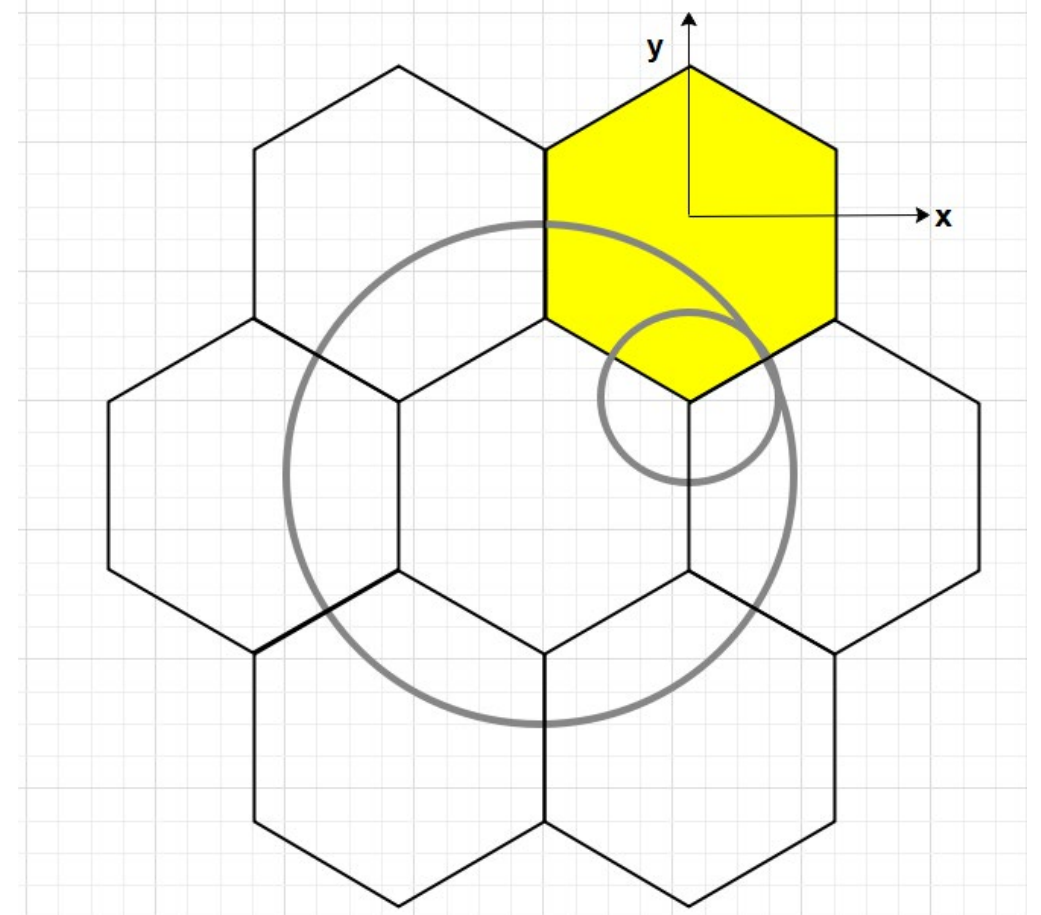
Examples

- From another program: some „track tiles“



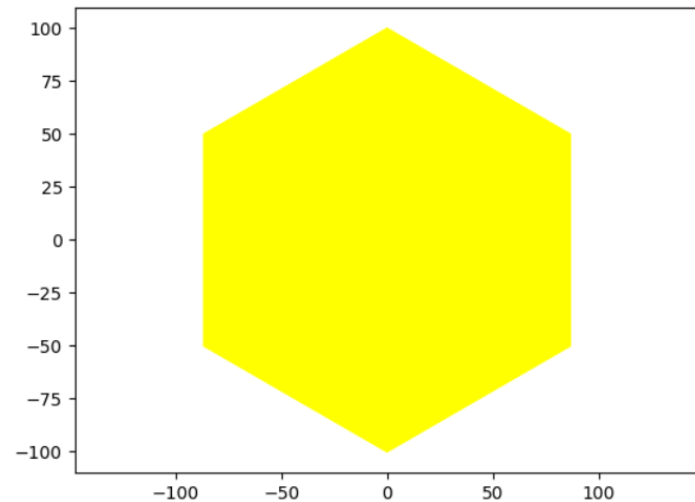
Construction of the tracks

- As we can see on the right: hexagons are beautiful for drawing.
- Again, all we need can be described from size s
- The radius of the smaller circle: $r = s / 2$
- The radius of the larger circle: $r = 1.5 * s$
- The center of the smaller circle = $(0, -s)$
- The center of the larger circle = $(-s, -1.5 * s)$
- All we have to do is „putting the elements together“



The basic polygon – made out of the corners

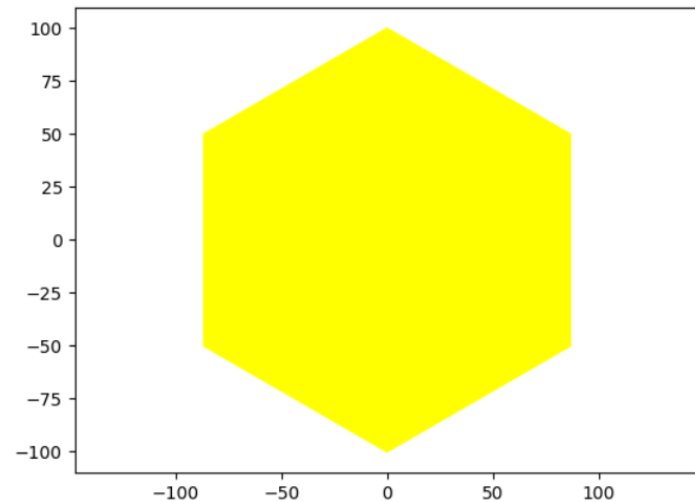
- Line 5 – 7: the „inputs“
- Line 9 – 11: calculating the values of the describing elements
- Line 14 -15: calculating the values of the coordinates of the corners
- Line 18: creating the polygon
- Line 19: drawing the polygon as patch



```
1 import matplotlib.pyplot as plt
2 from math import sqrt
3 from matplotlib.patches import Polygon
4
5 s = 100           # size of the elements (no unit!)
6 mx = 0           # center of the tile
7 my = 0           # center of the tile
8
9 r = s             # Radian outer circle
10 r2 = 0.5 * r     #
11 h = r2 * sqrt(3)  # radian inner circle
12
13 # corners starting at the top, clockwise
14 corners = [(mx + 0, my + r), (mx + h, my + r2), (mx + h, my - r2),
15            | (mx + 0, my - r), (mx - h, my - r2), (mx - h, my + r2)]
16
17 fig, ax = plt.subplots()
18 p1 = Polygon(corners, color="yellow")
19 ax.add_patch(p1)
20
21 plt.axis('equal')
22 plt.show()
23
```

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Learning programming = Learning decoupleling problems

- Question: in case I would like to draw a lot of polygons, what are the lines of code I need to do only this?
- Answer
 - Line 9 to 15 for really „calculating“ the corners
 - Line 18 für creating the Polygon
- The other lines?
 - Line 5 to 7 are just defining size and position of a single Polygon
 - Line 17 and 18 can be switched

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Introducing functions

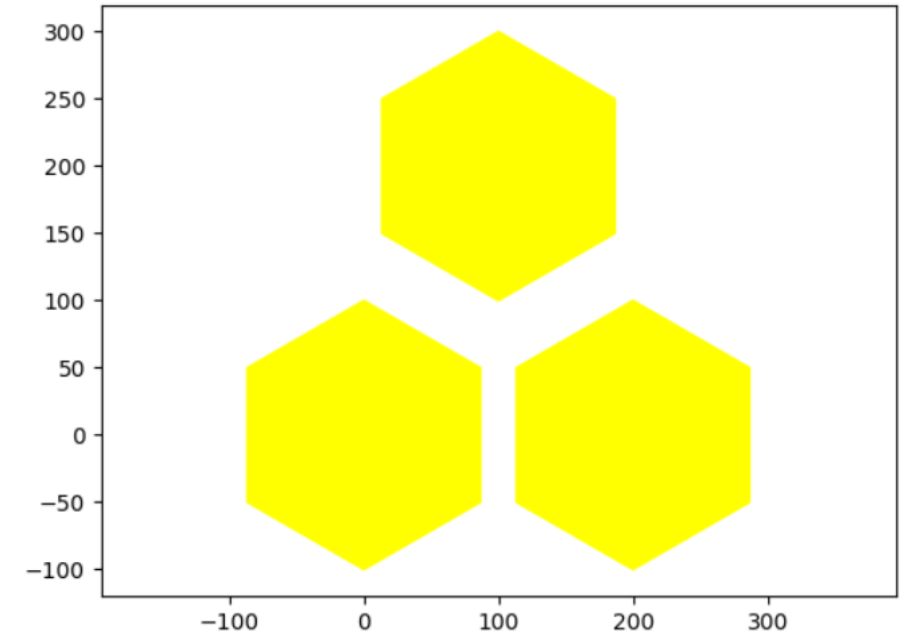
- Defining a function requires three decisions
 - What is the name of the function?
 - What are the parameter of the function for giving information into the function (from the caller)
 - What is the function returning (to the caller)
- The function has a general purpose. It is working for very values of `mx`, `my`, and `s`
- Line 5: name and parameter
- Line 15: returning the polygon
- Line 17: begin of the „main“ programm
- Line 19: Calling the function `drawTile`
- Remark:
the code of the function can be placed in an external file or module. It is then imported like the other libs in line 1 - 3

```
1 import matplotlib.pyplot as plt
2 from math import sqrt
3 from matplotlib.patches import Polygon
4
5 def drawTile(s, mx, my):
6     r = s                # Radian outer circle
7     r2 = 0.5 * r         #
8     h = r2 * sqrt(3)     # radian inner circle
9
10    # corners starting at the top, clockwise
11    corners = [(mx + 0, my + r), (mx + h, my + r2), (mx + h, my - r2),
12              | (mx + 0, my - r), (mx - h, my - r2), (mx - h, my + r2)]
13
14    p = Polygon(corners, color="yellow")
15    return p
16
17 fig, ax = plt.subplots()
18
19 p1 = drawTile(100, 0, 0)
20 ax.add_patch(p1)
21
22 plt.axis('equal')
23 plt.show()
24
```

Functions are somekind of sustainable: we are reusing code

- Calling a function again and again with different values for the parameter.
- Creating a „complex“ picture with a simple program.
- Can we make it more simple?
- How to use the code for drawing a playing board?

```
16
17 fig, ax = plt.subplots()
18
19 p1 = drawTile(100, 0, 0)
20 ax.add_patch(p1)
21
22 p2 = drawTile(100, 200, 0)
23 ax.add_patch(p2)
24
25 p3 = drawTile(100, 100, 200)
26 ax.add_patch(p3)
27
28 plt.axis('equal')
29 plt.show()
30
```



A playing board

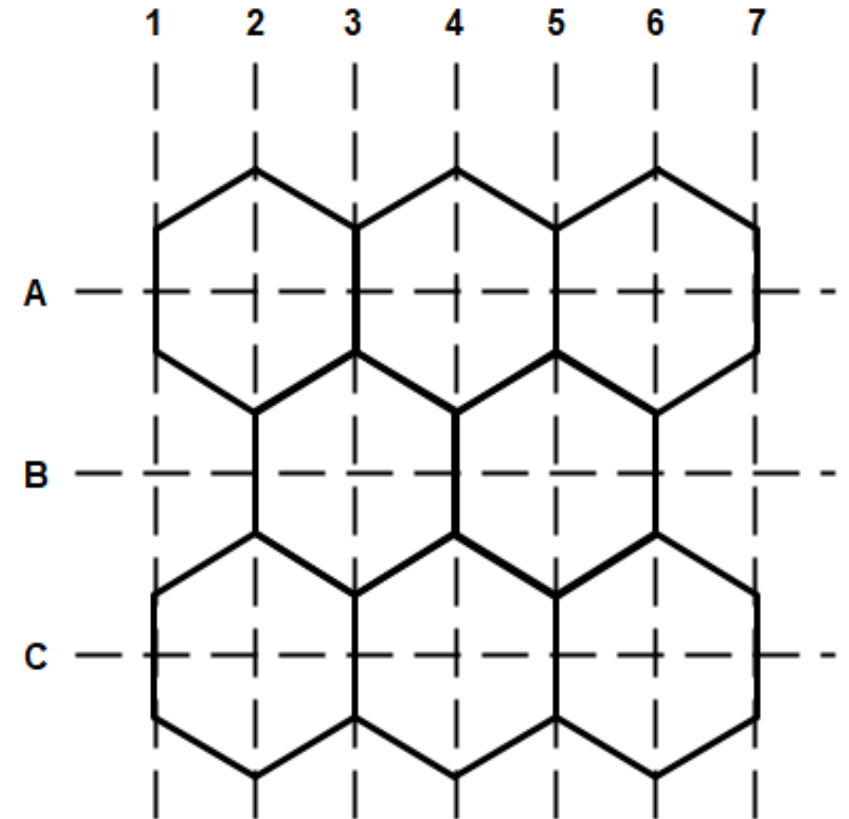
- Horizontal gap between axis 1. 2. 3. etc

$$dx = 0.5 * \sqrt{3} * s$$

- Vertical gap between axis A, B, C

$$dy = 1.5 * s$$

- Within a row the middle of tiles have the distance of $2 * dx$
- The middles for two rows have the distance of dy
- In odd rows (B) there is an
 - Offset of dx
 - The number of tiles is one less than in even rows (A, C)



Drawing a board

- Line 20 – 22: defining the size of the board
- Line 25 – 29: calculating the row specific parameter
- Line 22 – 23: calculating the coordinates of the middles
- A board is constructed out of rows and columns => 2 loops for iterating through all the positions
- Question: why is there a factor 0.9 in line 34???

```
18 fig, ax = plt.subplots()
19
20 nRows = 3      # number of rows
21 nCols = 3      # number of columns
22 size = 100     # size of a tile
23
24 for i in range(0, nRows, 1): # every row
25     offset = 0
26     cols = nCols
27     if i % 2 != 0:           # odd rows are different
28         offset = 0.5 * sqrt(3) * size
29         cols = nCols - 1
30
31     for j in range(0, cols, 1): # every column in the row
32         center_x = j * 0.5 * sqrt(3) * size * 2 + offset
33         center_y = i * 1.5 * size
34         p = drawTile(size * 0.9, center_x, center_y)
35         ax.add_patch(p)
36
37 plt.axis('equal')
38 plt.show()
```

Drawing a playing board – the result

